



# Science Virtual Learning

**MPI Physics 210**

**Rotational Dynamics 12**

**Angular Momentum**

**May 5, 2020**



Lesson: MPI Angular Momentum  
May 5, 2020

**Objective: To understand the concept of Angular Momentum and its conservation, and how to calculate it**

This video introduces the concept of angular momentum, and how it is calculated.

<https://youtu.be/SPsn9WL3h2I>

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Video: Angular Momentum 1



The Earth has a mass of  $5.98 \cdot 10^{24}$  kg, and a radius of  $6.37 \cdot 10^6$  m. It rotates once a day. Calculate the angular momentum of the Earth's rotation.

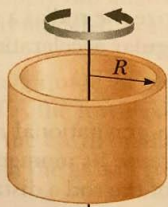
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Example from the first video

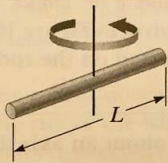


**TABLE 10.2** Moments of Inertia of Homogeneous Rigid Objects with Different Geometries

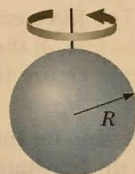
Hoop or thin cylindrical shell  
 $I_{CM} = MR^2$



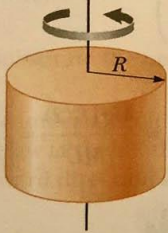
Long, thin rod with rotation axis through center  
 $I_{CM} = \frac{1}{12} ML^2$



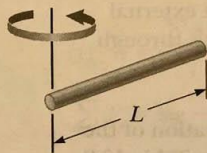
Solid sphere  
 $I_{CM} = \frac{2}{5} MR^2$



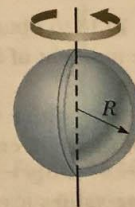
Solid cylinder or disk  
 $I_{CM} = \frac{1}{2} MR^2$



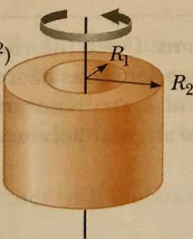
Long, thin rod with rotation axis through end  
 $I = \frac{1}{3} ML^2$



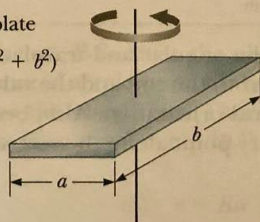
Thin spherical shell  
 $I_{CM} = \frac{2}{3} MR^2$



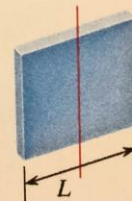
Hollow cylinder  
 $I_{CM} = \frac{1}{2} M(R_1^2 + R_2^2)$



Rectangular plate  
 $I_{CM} = \frac{1}{12} M(a^2 + b^2)$



Thin rectangular sheet, axis parallel to one edge and passing through center of other edge



$$I = \frac{1}{12} ML^2$$

Thin rectangular sheet, axis along one edge



$$I = \frac{1}{3} ML^2$$



# Moments of Inertia for Different Shapes

## Equation

## Missing

- |  |                |
|--|----------------|
| 1. $\omega_f = \omega_i + \alpha t$                    | $\Delta\theta$ |
| 2. $\Delta\theta = \frac{1}{2}(\omega_f + \omega_i)t$  | $\alpha$       |
| 3. $\Delta\theta = \omega_i t + \frac{1}{2}\alpha t^2$ | $\omega_f$     |
| 4. $\omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta$     | $t$            |
| 5. $\Delta\theta = \omega_f t - \frac{1}{2}\alpha t^2$ | $\omega_i$     |

# Rotational Motion Equations



Two disks are rotating about the same axis, one above the other. The top disk has a mass of 1.25 kg, and the bottom is 0.774 kg. They both have a radius of 0.118 m. The top one is rotating clockwise at 6.88 rad /s, and the bottom one is rotating counterclockwise at 9.46 rad/s. The top one falls onto the bottom one, and they stick together. What is the new angular velocity of the disks?

<https://youtu.be/WltQgVddYDs>

Example 2, and video



# Homework

1. A 75.0 kg person is standing on a stationary merry-go-round, 1.20 m from the axis. The merry-go-round has a 1.50 m radius, and a mass of 315 kg. The person then starts walking 1.30 m/s tangent to the circle (sideways, not inward or outward), so that she is walking counterclockwise around the merry-go-round. As a result, the merry-go-round begins spinning slowly in the opposite direction, clockwise.

- a) What was the total angular momentum BEFORE she started walking? (Should be easy.)
- b) What was the total angular momentum AFTER she started walking. (Should also be easy.)
- c) What was the woman's angular momentum after she started walking?
- d) What was the merry-go-round's angular momentum afterward? (Remember, you know the total from part b.)
- e) What was the angular velocity of the merry-go-round afterward?

- Try to solve the problem yourself, then watch the first part of the solution video:
- <https://youtu.be/X2BHAzcb-gs>





That's it!

